



**The Hong Kong University of Science and Technology**

**Department of Mathematics**

**MPhil THESIS EXAMINATION**

***A Simple Converging Embedding Method for the Laplace-Beltrami Operator on Implicit Surfaces***

*By*

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**ABSTRACT**

We propose a simple embedding method for computing the eigenvalues and eigenfunctions of the Laplace-Beltrami operator on implicit surfaces. The approach follows an embedding approach for solving the surface eikonal equation. We replace the differential operator on the interface with a typical Cartesian differential operator in the surface neighborhood and an extension operator on an outer layer of the computational tube. To observe a numerical convergence as the underlying mesh size approaches zero, we study different choices of the tube radius in the form of  $O(\Delta x^\gamma)$  for  $\gamma \in [0,1]$ . Our proposed algorithm is easy to implement and efficient. We will give some two- and three-dimensional numerical examples to demonstrate the effectiveness of our proposed approach.

**Date : 3 August 2022, Wednesday**

**Time : 02:00 p.m.**

**Venue : Online via ZOOM**

**ID: 932 5399 1486 (Passcode: 501724)**

**<https://hkust.zoom.us/j/93253991486>**

**Thesis Examination Committee**

**Chairman : Prof. Yang XIANG, MATH /HKUST**

**Thesis Supervisor : Prof. Shing Yu LEUNG, MATH/HKUST**

**Member : Prof. Xiaoping WANG, MATH/HKUST**

*(Open to all faculty and students)*

The student's thesis is now being displayed on the reception counter in the General Administration Office (Room 3461).